

# Statistics

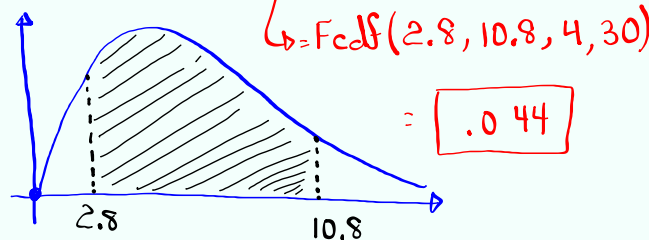
## Lecture 27



Feb 19-8:47 AM

Review on F-Dist.:

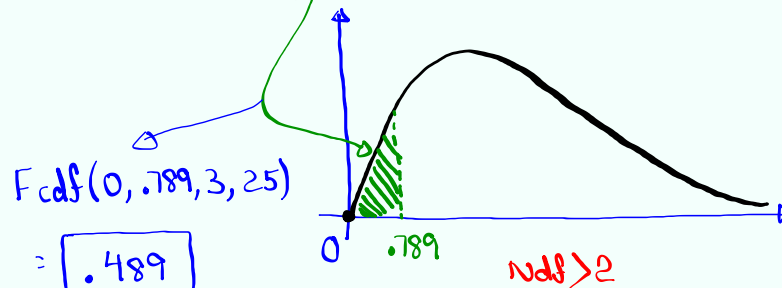
find  $P(2.8 < F < 10.8)$  with  $Ndf=4$  &  $Ddf=30$ .



$= \boxed{.044}$

$Ndf > 2$

find  $P(F < .789)$  with  $Ndf=3$  &  $Ddf=25$ .



$= \boxed{.489}$

$Ndf > 2$

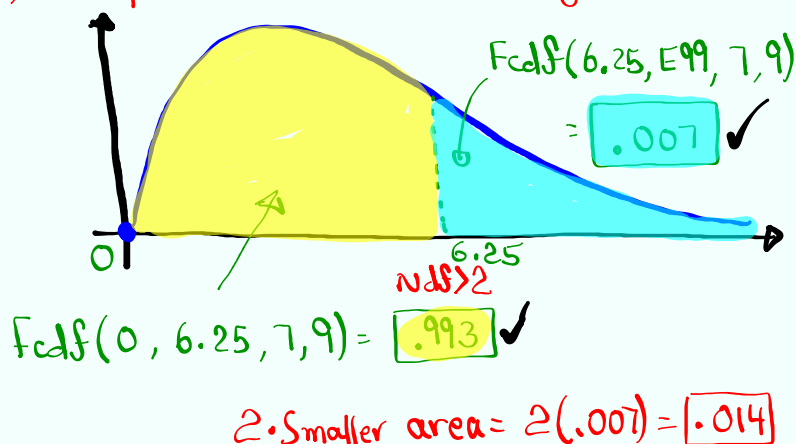
Dec 8-10:37 AM

Given  $F = 6.25$   $Ndf = 7$  &  $Ddf = 9$

1) find the area to its right.

2) find the area to its left.

3) Multiply the Smaller area by 2.



Dec 8-10:43 AM

Comparing Two Population Standard deviations: SG 29

$$H_0: \sigma_1 = \sigma_2$$

$$H_0: \sigma_1 \leq \sigma_2$$

$$H_0: \sigma_1 \geq \sigma_2$$

$$H_1: \sigma_1 \neq \sigma_2$$

$$H_1: \sigma_1 > \sigma_2$$

$$H_1: \sigma_1 < \sigma_2$$

TTT

RTT

LTT

| Sample 1 | Sample 2 |
|----------|----------|
| $n_1 =$  | $n_2 =$  |
| $S_1 =$  | $S_2 =$  |

$$1) S_1 > S_2$$

$$2) Ndf = n_1 - 1, Ddf = n_2 - 1$$

$$3) CTS \quad F = \frac{S_1^2}{S_2^2}$$

CTS F

P-value P

STAT

TESTS

2-SampF Test

inpt:

Stats

Proceed with  
P-value Method.

Dec 8-10:51 AM

Use the chart below to test the claim that  $\sigma_1 = \sigma_2$ .  
 $\text{No } \alpha \rightarrow .05$

| Sample 1  | Sample 2   |
|-----------|------------|
| $n_1 = 8$ | $n_2 = 10$ |
| $s_1 = 6$ | $s_2 = 4$  |

$H_0: \sigma_1 = \sigma_2$  claim

$H_1: \sigma_1 \neq \sigma_2$  TTT

1)  $s_1 > s_2$  ✓

2)  $Ndf = n_1 - 1 = 7$

$Ddf = n_2 - 1 = 9$

3) CTS  $F = \frac{s_1^2}{s_2^2} = \frac{6^2}{4^2} = 2.25$

4) **STAT** **2-Samp F Test**  
**TESTS** inpt: **Stats**

P-value Method

$P\text{-value} > \alpha$   
 $.256 > .05$

CTS  $F = 2.25$   
 P-value  $P = .256$  ✓

$H_0$  valid valid claim

$H_1$  invalid

FTR the claim

Dec 8-10:58 AM

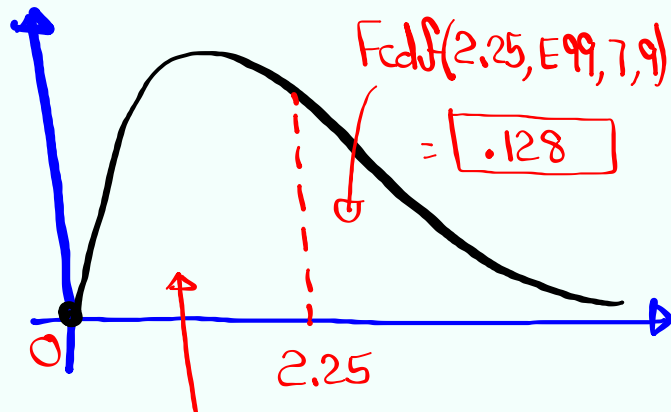
CTS  $F = 2.25$

$Ndf = 7$

$Ddf = 9$

TTT

Find p-value.



$Fcdf(0, 2.25, 7, 9) = .872$

P-value = 2 • Smaller area

$= 2 (.128) = .256$

Dec 8-11:08 AM

Standard deviation of ages of 10 randomly  
Selected female students was 8 yrs.  
 $n=10$   $S=8$

Standard deviation of ages of 12 randomly  
Selected male students was 5 yrs.  
 $n=12$   $S=5$

use  $\alpha=.1$  to test the claim that two pop.  
standard deviations are not equal.

$$H_0: \sigma_1 = \sigma_2$$

$$\sigma_1 \neq \sigma_2$$

$$H_1: \sigma_1 \neq \sigma_2 \text{ claim, TTT}$$

| Female   | male     |
|----------|----------|
| $n_1=10$ | $n_2=12$ |
| $S_1=8$  | $S_2=5$  |

$$S_1 > S_2 \checkmark$$

$$\text{ndf} = n_1 - 1 = 9, \text{Ddf} = n_2 - 1 = 11$$

$$\text{CTS } F = \frac{S_1^2}{S_2^2} = \frac{8^2}{5^2} = 2.56$$

$$\text{CTS } F = 2.56$$

$$\text{P-value } P = .144$$

2-Samp F Test

$$\text{P-value} > \alpha$$

$$.144$$

$$.1$$

$H_0$  valid

$H_1$  invalid

Invalid claim  
Reject  
the claim

Dec 8-11:12 AM

|       |           |           |
|-------|-----------|-----------|
| Given | Sample 1  | Sample 2  |
|       | $n_1 = 8$ | $n_2 = 8$ |
|       | $S_1 = 8$ | $S_2 = 2$ |

Test the claim that  $\sigma_1 > \sigma_2$ .

No  $\alpha \rightarrow .05$

$$H_0: \sigma_1 \leq \sigma_2$$

$$H_1: \sigma_1 > \sigma_2 \text{ claim, RTT}$$

$$S_1 > S_2 \checkmark$$

$$\text{ndf} = n_1 - 1 = 7$$

$$\text{Ddf} = n_2 - 1 = 7$$

$$\text{CTS } F = 16$$

$$\text{P-value } P = 8.181 \times 10^{-4}$$

2-Samp F Test

FTR the claim

$$\text{P-value} \leq \alpha$$

$H_0$  invalid

$H_1$  valid

valid claim

$$\text{CTS } F = \frac{S_1^2}{S_2^2} = \frac{8^2}{2^2} = 16$$

Dec 8-11:24 AM



Comparing At least 3 population Means. SG 33

Method: ANOVA  
(Analysis of Variance)

$$H_0: \mu_1 = \mu_2 = \mu_3 = \dots = \mu_K$$

$H_1$ : At least one mean is different. RTT

$$Ndf = K - 1$$

$K \Rightarrow$  # of groups

$$Ddf = n - K$$

$n \Rightarrow$  Total Sample Size

CTS F

STAT

First save

$\Rightarrow$

TESTS

all data elements

P-value P

ANOVA

in L1, L2, L3, ...

Proceed with P-value Method.

Dec 8-11:33 AM

Ages of randomly selected students are given below:

| ELAC       | Mt. SAC     | Chaffey     |
|------------|-------------|-------------|
| 25, 28, 19 | 23, 27, 32, | 21, 28, 33, |
| 20, 30, 18 | 18, 25, 30  | 19, 25      |

Test the claim that all means are equal.

No  $\alpha \rightarrow .05$

$H_0: \mu_1 = \mu_2 = \mu_3$  Claim

ELAC  $\rightarrow$  L1

$H_1$ : At least one mean is different. RTT

Mt. SAC  $\rightarrow$  L2

$$K=3 \rightarrow Ndf=K-1=2$$

Chaffey  $\rightarrow$  L3

$$n=17 \rightarrow Ddf=n-K=14$$

STAT

TESTS ANOVA(L1, L2, L3 enter)

CTS F = .371

P-value  $> \alpha$

P-value P = .697

$H_0$  valid  $H_1$  invalid

valid claim

FTR the claim

Dec 8-11:39 AM

Exam Scores from 4 of my classes are given below

| L1<br>In-Person | L2<br>Monday only | L3<br>Tuesday only | L4<br>Online |
|-----------------|-------------------|--------------------|--------------|
| 75 83 95        | 68 98 88          | 75 85              | 92 96        |
| 70 80           | 58 78             | 98 100             | 100 90       |
|                 |                   | 80                 | 88 98        |

$k=4$     $ndf=k-1=3$   
 $n=21$     $Ddf=n-k=17$

Use  $\alpha=.01$  to test the claim that all pop. means are equal.

$H_0: \mu_1 = \mu_2 = \mu_3 = \mu_4$  claim  
 $H_1$ : At least one mean is different. RTT

CTS  $F = 2.484$   
 P-value  $P = .096$

$P\text{-value} > \alpha$   
 $.096 > .01$   
 $H_0$  valid  
 $H_1$  invalid  
 valid claim

ANOVA(L1, L2, L3, L4)

If  $\alpha = .1$ , then  
 $P\text{-value} \leq \alpha$   
 $.096 \leq .1$   
 $H_0$  invalid  
 $H_1$  valid  
 Invalid claim → Reject the claim

FTR the claim

Dec 8-11:51 AM

Gas Prices were randomly selected from different gas stations in 3 major Cities in Ca.

| L1<br>Los Angeles | L2<br>San Francisco | L3<br>San Diego |
|-------------------|---------------------|-----------------|
| 4.25 4.85         | 4.85 5.25           | 4.29 4.39       |
| 4.75 4.05         | 5.15 5.85           | 4.49 3.99       |
| 4.95              | 6.15                | 3.89            |

Test the claim that not all means are equal.

$H_0: \mu_1 = \mu_2 = \mu_3$   
 $H_1$ : At least one mean is different claim, RTT

$K=3$     $ndf=k-1=2$   
 $n=15$     $Ddf=n-k=12$

CTS  $F = 11.992$   
 P-value  $P = .001$

ANOVA(L1, L2, L3)

$P\text{-value} \leq \alpha$   
 $H_0$  invalid  
 $H_1$  valid → valid claim → FTR the claim.

S& 29 & 33 ✓

Dec 8-12:06 PM